

**THE EMBODIMENTS OF THE INVENTION IN WHICH AN EXCLUSIVE  
PROPERTY OR PRIVILEGE IS CLAIMED ARE DEFINED AS FOLLOWS:**

1. A method of providing a point multiple in an elliptic curve cryptosystem, said point multiple being derived from a scalar and a point on an elliptic curve having an equation of the form  $y^2 + xy = x^3 + a_1x^2 + 1$ , where  $a_1$  is either 0 or 1, said method comprising the steps of:
  - a) obtaining a pair of coefficients derived from a truncator of said elliptic curve;
  - b) computing a representation of said scalar from said pair of coefficients, said scalar, and said truncator of said elliptic curve;
  - c) computing said point multiple using said representation of said scalar and a Frobenius mapping  $\tau$  .;
  - d) providing said point multiple to said elliptic curve cryptosystem.
2. A method according to claim 1, wherein said pair of coefficients corresponds to an approximation of the inverse of said truncator.
3. A method according to claim 2, wherein said approximation is determined by a significance parameter.
4. A method according to claim 1, wherein said representation of said scalar is equivalent to said scalar modulo said truncator.
5. A method according to claim 2, further comprising the step of computing a quotient derived from said pair of coefficients and said scalar and using said quotient to perform the step of computing said representation of said scalar.
6. A method according to claim 5, wherein said quotient is equivalent to a product of said scalar and said approximation of said inverse of said truncator.

7. A method according to claim 6, wherein said representation of said scalar is equivalent to a remainder after division of said scalar by said truncator.

8. A method according to claim 1, wherein said truncator is  $\frac{\tau^m - 1}{\tau - 1}$

5 9. A method of computing a key derived from a scalar and a point on an elliptic curve having an equation of the form  $y^2 + xy = x^3 + a_1x^2 + 1$ , where  $a_1$  is either 0 or 1, said method comprising the steps of:

- a) obtaining a pair of coefficients derived from a truncator of said elliptic curve;
- b) computing a representation of said scalar from said pair of coefficients, said scalar, and said truncator of said elliptic curve;
- c) computing said point multiple using said representation of said scalar and a Frobenius mapping  $\tau$ .

10. In a method of computing an elliptic curve digital signature requiring a point multiple, the improvement comprising computing said point multiple by the steps of:

- a) obtaining a pair of coefficients derived from a truncator of said elliptic curve;
- b) computing a representation of said scalar from said pair of coefficients, said scalar, and said truncator of said elliptic curve;
- c) computing said point multiple using said representation of said scalar and said endomorphism of said elliptic curve.

11. A data carrier containing computer executable instructions for performing a method according to claim 1.

12. A cryptographic system performing a method according to claim 1.